

## Algebra 2 Equation Development 2.1

(Key)

Solve, check, and graph the following equations and inequalities.

1)  $4d^3 + 47 = -61$

$$\begin{array}{r} -47 \\ -47 \\ \hline 4d^3 = -108 \end{array}$$

$$\begin{array}{r} 4 \\ 4 \end{array}$$

$$d^3 = -27$$

$$\boxed{x = -4}$$

$$\sqrt[3]{d^3} = \sqrt[3]{-27}$$

$$\boxed{d = -3}$$

$$\checkmark 4(-3)^3 + 47 = -61$$

$$4(-27) + 47 = -61$$

$$-108 + 47 = -61$$

$$-61 = -61 \checkmark$$

$$\begin{array}{r} -6k \\ -6k \\ \hline 163 = 53 + 11k \end{array}$$

$$\begin{array}{r} -53 \\ -53 \end{array}$$

$$\begin{array}{r} 110 \\ 11 \\ \hline 11 \end{array} = \frac{11k}{11}$$

$$\boxed{10 = k}$$

$$\boxed{x = -9}$$

$$\checkmark 163 + 6(10) = 53 + 17(10)$$

$$163 + 60 = 53 + 170$$

$$223 = 223 \checkmark$$



5)  $4t + 5 \geq 21$

6)  $-3m - 7 < 14$

7)  $12x - 7x - 16 < -56$

8)  $3(-2x + 11) \leq 129$

$$\boxed{t \geq 4}$$

$$\begin{array}{r} +7 \quad +7 \\ \hline \underline{-3m < 21} \\ -3 \quad -3 \end{array}$$

$$\boxed{x < -8}$$

$$\begin{array}{r} -6x + 33 \leq 129 \\ \hline \underline{-33 \quad -33} \\ -6x \leq 96 \\ -6 \quad -6 \end{array}$$

$$\boxed{x \geq -16}$$



$$\boxed{m > -7}$$



$$\begin{array}{r} \checkmark 3(-2(0) + 11) \leq 129 \\ 3(11) \leq 129 \\ 33 \leq 129 \checkmark \end{array}$$

$$\begin{array}{r} \checkmark -3(0) - 7 < 14 \\ -7 < 14 \checkmark \end{array}$$

9)  $x + \frac{2}{3} = \frac{5}{3}$

$$\begin{array}{r} -2/3 \quad -2/3 \\ \hline \end{array}$$

10)  $x - \frac{1}{4} = \frac{3}{4}$

11)  $x + \frac{3}{2} = \frac{1}{3}$

12)  $x - \frac{3}{4} = \frac{1}{8}$

$$\begin{array}{r} -3/2 \quad -3/2 \\ \hline \end{array}$$

$$x = 2/6 - 9/6$$

$$\boxed{x = 3/3 = 1}$$

$$\boxed{x = 1}$$

$$\boxed{x = -7/6}$$

$$\boxed{x = 7/8}$$

$$\checkmark (3/3) + 2/3 = 5/3$$

$$\begin{array}{r} 5/3 = 5/3 \checkmark \\ \hline \end{array}$$



$$\checkmark (-7/6) + 3/2 = 1/3$$

$$-7/6 + 9/6 = 1/3$$

$$2/6 = 1/3$$

$$1/3 = 1/3 \checkmark$$



$$13) \frac{1}{4}x = \frac{1}{16}$$

$$14) \frac{2}{9}x = \frac{9}{2}$$

$$15) \frac{3}{7}x = \frac{4}{9}$$

$$16) \frac{3}{8}x = \frac{5}{12}$$

$$\left(\frac{9}{2}\right)\frac{2}{9}x = \frac{9}{2}\left(\frac{9}{2}\right)$$

$$\left(\frac{8}{3}\right)\frac{3}{8}x = \frac{5}{12}\left(\frac{8}{3}\right)$$

$$x = 1/4$$

$$x = 81/4$$

$$x = 28/27$$

$$x = 10/9$$

$$\checkmark(2/9)(81/4) = 9/2$$

$$9/2 = 9/2\checkmark$$

$$\begin{array}{c} \\ \hline 0 & \quad 81/4 \\ & \bullet \end{array}$$

$$\checkmark(3/8)(10/9) = 5/12$$

$$5/12 = 5/12\checkmark$$

$$\begin{array}{c} \\ \hline 0 & \quad 10/9 \\ & \bullet \end{array}$$

Evaluate each expression if  $x = 3$ ,  $y = -6$ , and  $z = -1.5$

$$17) |-5x|$$

$$18) |-9y|$$

$$19) |6z|$$

$$20) |4xy|$$

$$21) -|-2yz|$$

$$\begin{array}{l} |-5(3)| = |-15| \\ \boxed{= 15} \end{array}$$

$$54$$

$$9$$

$$72$$

$$\begin{array}{l} -|-2(-6)(-1.5)| \\ = -|-18| = -(18) \\ \boxed{= -18} \end{array}$$

Solve, check, and graph the following equations.

$$22) |w| = 5$$

$$23) |x + 4| = 13$$

$$24) |b - 7| = -4$$

$$25) 3|t - 5| = 9$$

$$\begin{array}{rcl} x + 4 = 13 & x + 4 = -13 \\ -4 \quad -4 & -4 \quad -4 \end{array}$$

$$\boxed{w = 5, -5}$$

$$\boxed{x = 9 \quad x = -17}$$

$$\emptyset, \text{No solution}$$

$$|t - 5| = 3$$

$$\begin{array}{ll} \checkmark |(9) + 4| = 13 & |(-17) + 4| = 13 \\ |13| = 13 & |-13| = 13 \\ 13 = 13 & 13 = 13\checkmark \end{array}$$

$$\begin{array}{c} \bullet \\ \hline -17 & 0 & 9 \\ & \bullet \end{array}$$

$$\begin{array}{ll} t - 5 = 3 & t - 5 = -3 \\ +5 \quad +5 & +5 \quad +5 \end{array}$$

$$\boxed{t = 8 \quad t = 2}$$

$$\begin{array}{ll} \checkmark 3|(8) - 5| = 9 & 3|(2) - 5| = 9 \\ 3|3| = 9 & 3|-3| = 9 \\ 3(3) = 9 & 3(3) = 9 \\ 9 = 9 & 9 = 9\checkmark \end{array}$$

$$\begin{array}{c} \bullet \\ \hline 0 & 2 & 8 \\ & \bullet \end{array}$$

Solve the following literal equations in terms of the underlined variable.

$$26) \underline{a} + 5 = b$$

$$27) \underline{c} + d = 12$$

$$28) 5\underline{f} + g = 8$$

$$29) \frac{\underline{j}}{2} + k = 7$$

$$\frac{-5}{a} = \frac{-5}{b - 5}$$

$$\boxed{a = b - 5}$$

$$\boxed{c = -d + 12}$$

$$\frac{-g}{5} = \frac{-g}{5}$$

$$\begin{array}{l} \frac{5f}{5} = \frac{-g + 8}{5} \\ f = \frac{-g}{5} + \frac{8}{5} \end{array}$$

$$\boxed{j = -2k + 14}$$

$$30) \quad \frac{4}{5}p = 3q$$

$$31) \quad tv = 9$$

$$32) \quad \frac{3}{8}xyz = w$$

$$33) \quad 3a + 2b = 5$$

$$p = \frac{15q}{4}$$

$$t = \frac{9}{v}$$

$$x = \frac{8w}{3yz}$$

$$a = \frac{-2b + 5}{3}$$

$$a = \frac{-2b}{3} + \frac{5}{3}$$